

CLASS: M.Sc. MATHEMATICS

15A/ 321

St. JOSEPH'S COLLEGE (AUTONOMOUS) TIRUCHIRAPPALLI – 620 002

SEMESTER EXAMINATIONS – APRIL 2015

TIME: 3 Hrs.

MAXIMUM MARKS: 100

SEM	SET	PAPER CODE	TITLE OF THE PAPER
IV	2013	12PMA4202A	AUTOMATA THEORY

SECTION – A

Answer all the questions:

10 x 2 = 20

1. Define a finite automation.
2. Define regular language.
3. If $L_1 = \{10, 1\}$ and $L_2 = \{011, 11\}$, find L_1L_2 .
4. State the relationship between derivation trees and derivations.
5. What is a stack?
6. Define accepted languages.
7. Write the regular – expression construction rules.
8. Define a recognizer for a language.
9. Define a parser for a grammar.
10. What are the four possible actions a shift – reduce parser can make?

SECTION – B

Answer all the questions:

5 x 7 = 35

11. a. Explain non deterministic finite automaton with an example.

OR

- b. Let $M = (\{q_0, q_1\}, \{0, 1\}, \delta, q_0, \{q_1\})$ be an NFA where $\delta(q_0, 0) = \{q_0, q_1\}$, $\delta(q_0, 1) = \{q_1\}$, $\delta(q_1, 0) = \phi$ and $\delta(q_1, 1) = \{q_0, q_1\}$. Construct a DFA $M' = (Q, \{0,1\}, \delta', [q_0], F)$ accepting $L(M)$.
12. a. If L is accepted by a DFA, prove that L is denoted by a regular expression.

OR

- b. Explain derivation tree with an example.
13. a. Give a PDA that accepts $\{ww^R \mid w \in (0+1)^*\}$.

OR

- b. If L is $L(M_2)$ for some PDA M_2 , prove that L is $N(M_1)$ for some PDA M_1 .
14. a. Write the need for lexical analysis.

OR

- b. Write an algorithm for minimizing the number of states of a DFA.
15. a. Write an algorithm for computing operator – precedence relations.

OR

- b. Write an algorithm for constructing a predictive parsing table.

SECTION – C

Answer any THREE questions:

3 x 15 = 45

16. If L is a set accepted by a non deterministic finite automaton, prove that there exists a deterministic finite automaton that accepts L .
17. State and prove the theorem on Chomsky normal form.

18. If L is $N(M)$ for some PDA M , prove that L is a context free language.
19. Write the algorithm for constructing an NFA from a regular expression.
20. Explain top-down parsing with example and write some of its difficulties.
